

Remarks on Precondition Generation (Footprints, Abduction, etc)

Peter O'Hearn
SNU, 12 May 2009

Based on joint work with Cristiano Calcagno,
Dino Distefano, Hongseok Yang

Recall from Yesterday how we used Abduction
to generate specifications (preconditions) for
bare code

Abduction Example: Inferring a pre/post pair

1 void p(list-item *y) {	emp	list(y)(Inferred Pre)
2 list-item *x;		
3 x=malloc(sizeof(list-item));		
4 x→tail = 0;	x ↦ 0	
5 foo(x,y);	list(x)	
6 return(x); }		list(ret)(Inferred Post)

Abductive Inference: $x \mapsto 0 * \text{list}(y) \vdash \text{list}(x) * \text{list}(y)$

Given Summary/spec: $[\text{list}(x) * \text{list}(y)] \text{foo}(x, y) [\text{list}(x)]$

Today we will talk a bit more in depth about that,
including some of the trickinesses.

This talk is intended to be informal. Feel free to ask
questions (if I can't answer, I will refer you to...)

Example

```
{emp}  
x=nil;  
while (-){  
    new(y);  
    y->tl = x;  
    x=y;  
}
```

Calculated Loop Invariant

∨

∨

Example

```
{emp}
x=nil;
while (-){  x = nil ^ emp
            new(y);
            y ->tl = x;
            x=y;
}
```

Calculated Loop Invariant

$x = \text{nil} \wedge \text{emp}$

∇

∇

Example

```
{emp}
x=nil;
while (-){  x ↦ nil
            new(y);
            y ->tl = x;
            x=y;
}
```

Calculated Loop Invariant

$x = \text{nil} \wedge \text{emp}$

$\vee x \mapsto \text{nil}$

\vee

Example

```
{emp}
x=nil;
while (-){    x ↦ x' * x' ↦ nil
    new(y);
    y ->tl = x;
    x=y;
}
```

Calculated Loop Invariant

$x = \text{nil} \wedge \text{emp}$

∨ $x \mapsto \text{nil}$

∨

Example

```
{emp}
x=nil;
while (- ){    ls(x, nil)
    new(y);
    y ->tl = x;
    x=y;
}
```

Calculated Loop Invariant

$x = \text{nil} \wedge \text{emp}$

$\vee x \mapsto \text{nil}$

$\vee \text{ls}(x, \text{nil})$

Example

```
{emp}
x=nil;
while (-){
    x  $\mapsto$  x' * ls(x', nil)
    new(y);
    y -> tl = x;
    x=y;
}
```

Calculated Loop Invariant

```
x = nil  $\wedge$  emp
 $\vee$  x  $\mapsto$  nil
 $\vee$  ls(x, nil)
```

Example

```
{emp}
x=nil;
while (-){      ls(x,nil)
    new(y);
    y->tl = x;
    x=y;
}
```

Calculated Loop Invariant

$x = \text{nil} \wedge \text{emp}$

$\vee x \mapsto \text{nil}$

$\vee \text{ls}(x, \text{nil})$

Example

```
{emp}  
x=nil;  
while (-){      ls(x,nil)  
    new(y);  
    y->tl = x;  
    x=y;  
}
```

Calculated Loop Invariant

```
x = nil  $\wedge$  emp  
 $\vee$  x  $\mapsto$  nil  
 $\vee$  ls(x,nil)
```

Fixed-point reached!

Cooking a Program Analyzer

1. Just write an interpreter. (Well, an *abstract* interpreter.)
2. Symbolically execute statements using in-place reasoning (all true Hoare triples).
3. Interpret while loops by using abstractin rules like

$$\text{ls}(x, t') * \text{list}(t') \vdash \text{list}(x)$$

to automatically find loop invariants. This uses the rule of consequence on the right to find the invariant for the while rule

$$\frac{\{P\}C\{Q\} \quad Q \vdash Q'}{\{P\}C\{Q'\}} \quad \frac{\{I \wedge B\}C\{I\}}{\{I\}\text{while } B \text{ do } \{I \wedge \neg B\}}$$

4. A terminating run of the interpreter will give us a **proof** of assertions at all program points.

Abstraction, fixed-points, and Precondition Generation

```
1:  while (c!=NULL) {
2:      t=c;
3:      c=c->t1;
4:      free(t);
5:  }
```

Discovered Precondition: $c == c_ \wedge \text{lseg}(c_ , \text{NULL})$

	Current Heap	Footprint Heap
First iteration		
pre:	$c \neq \text{NULL} \wedge c == c_ \wedge t == c_ \wedge \text{emp}$	emp
post:	$t \neq \text{NULL} \wedge c == c1_ \wedge t == c_ \wedge c_ \mapsto c1_$	$c_ \mapsto c1_$
Second Iteration		
pre:	$c \neq \text{NULL} \wedge c == c1_ \wedge t == c1_ \wedge \text{emp}$	$c_ \mapsto c1_$
post:	$t \neq \text{NULL} \wedge c == c2_ \wedge t == c1_ \wedge c1_ \mapsto c2_$	$c_ \mapsto c1_ * c1_ \mapsto c2_$
abs post:	$t \neq \text{NULL} \wedge c == c2_ \wedge t == c1_ \wedge c1_ \mapsto c2_$	$\text{lseg}(c_ , c2_)$
Third Iteration		
pre:	$c \neq \text{NULL} \wedge c == c2_ \wedge t == c2_ \wedge \text{emp}$	$\text{lseg}(c_ , c2_)$
post:	$t \neq \text{NULL} \wedge c == c3_ \wedge t == c2_ \wedge c2_ \mapsto c3_$	$\text{lseg}(c_ , c2_) * c2_ \mapsto c3_$
abs post:	$t \neq \text{NULL} \wedge c == c3_ \wedge t == c2_ \wedge c2_ \mapsto c3_$	$\text{lseg}(c_ , c3_)$

Fig. 2. Pre and Post States at line 3 during footprint analysis of `delete_list`

	Current Heap	Footprint Heap
First iteration		
pre:	$c \neq \text{NULL} \wedge c == c_ \wedge t == c_ \wedge \text{emp}$	emp
post:	$t \neq \text{NULL} \wedge c == c1_ \wedge t == c_ \wedge c_ \mapsto c1_$	$c_ \mapsto c1_$
Second Iteration		
pre:	$c \neq \text{NULL} \wedge c == c1_ \wedge t == c1_ \wedge \text{emp}$	$c_ \mapsto c1_$
post:	$t \neq \text{NULL} \wedge c == c2_ \wedge t == c1_ \wedge c1_ \mapsto c2_$	$c_ \mapsto c1_ * c1_ \mapsto c2_$
abs post:	$t \neq \text{NULL} \wedge c == c2_ \wedge t == c1_ \wedge c1_ \mapsto c2_$	$\text{lseg}(c_, c2_)$
Third Iteration		
pre:	$c \neq \text{NULL} \wedge c == c2_ \wedge t == c2_ \wedge \text{emp}$	$\text{lseg}(c_, c2_)$
post:	$t \neq \text{NULL} \wedge c == c3_ \wedge t == c2_ \wedge c2_ \mapsto c3_$	$\text{lseg}(c_, c2_)* c2_ \mapsto c3_$
abs post:	$t \neq \text{NULL} \wedge c == c3_ \wedge t == c2_ \wedge c2_ \mapsto c3_$	$\text{lseg}(c_, c3_)$

Fig. 2. Pre and Post States at line 3 during footprint analysis of `delete_list`

```

1: while (c!=NULL) {
2:     t=c;
3:     c=c->t1;
4:     free(t);
5: }

```

Discovered Precondition: $c == c_ \wedge \text{lseg}(c_, \text{NULL})$

Finally, we can exit the loop by removing “ $c2_+ \mapsto c3_+$ ” from the current heap in the `free` command, and adding the negation of the loop conditional to the heap and footprint, and forgetting about τ because it is a local variable. A bit of logic tells us that the footprint part is equivalent to $c3_+ == \text{NULL} \wedge \text{lseg}(c_+, c3_+)$, and when we add this to the initial precondition $c == c_+$ we obtain the overall precondition pictured in Figure 1.

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to automatically find loop invariants. This uses the rule of consequence on the right to find the invariant for the while rule

$$\frac{\{P\}C\{Q\} \quad Q \vdash Q'}{\{P\}C\{Q'\}} \quad \frac{\{I \wedge B\}C\{I\}}{\{I\}\text{while } B \text{ do } \{I \wedge \neg B\}}$$

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Cooking a Program Analyzer

1. Just write an interpreter. (Well, an *abstract* interpreter.)
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$$ls(x, t') * list(t') \vdash list(x)$$

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$$\begin{array}{c}
 P|-P' \quad \{P\}C\{Q\} \\
 \hline
 \{P'\}C\{Q\}
 \end{array}
 \quad ??
 \quad
 \frac{\{P\}C\{Q\} \quad Q \vdash Q'}{\{P\}C\{Q'\}}
 \quad
 \frac{\{I \wedge B\}C\{I\}}{\{I\} \text{while } B \text{ do } \{I \wedge \neg B\}}$$

4. A terminating run of the interpreter will give us a **proof** of assertions at all program points.

Implications for Overapproximating Analysis

$$\frac{P|-P' \quad \{P\}C\{Q\}}{\text{-----}??} \{P'\}C\{Q\}$$

This rule is unsound

So, we generate “candidate” preconditions, then filter unsafe ones out using sound forwards analysis

`delete-doublestar` uses the usual C trick of double indirection to avoid unnecessary checking for the first element, when deleting an element from a list.

```
void delete-doublestar(nodeT **listP, elementT value)
{
    nodeT *currP, *prevP;
    prevP=NULL;
    for (currP=*listP; currP!=NULL; prevP=currP, currP=currP->next) {
        if (currP->element==value) { /* Found it. */
            if (prevP==NULL) *listP=currP->next;
            else prevP->next=currP->next;
            free(currP);
        }
    }
}
```

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        if (currP->element==value) { /* Found it. */
            if (prevP==NULL) *listP=currP->next;
            else prevP->next=currP->next;
            free(currP);
        }
    }
}
```

What is the Footprint?

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        if (currP->element==value) { /* Found it. */
            if (prevP==NULL) *listP=currP->next;
            else prevP->next=currP->next;
            free(currP);
        }
    }
}
```

What is the Footprint?

```
listP ↦ x_*ls(x_,x1_)*x1_ ↦ element:value,
listP ↦ x_*ls(x_,NULL)
```


Program	Time (s)	Memory	# of Disjuncts	Unsafe Pre	Discovered Precondition
append.c	0.03501	0.74Mb	4	0	$ls(x, NULL)$
append-dispose.c	0.09966	0.74Mb	17	0	$ls(x, NULL) * ls(y, NULL)$
copy.c	0.03076	0.74Mb	4	0	$ls(c, NULL)$
create.c	0.01370	0.49Mb	1	0	emp
delete-doublestar.c	0.04521	0.49Mb	10	0	$listP \mapsto x * ls(x, x1) * x1 \mapsto element : value,$ $listP \mapsto x * ls(x, NULL)$
delete-all.c	0.01357	0.49Mb	4	0	$ls(c, NULL)$
delete-all-circular.c	0.01564	0.49Mb	3	0	$c \mapsto c * ls(c, c)$
delete-lseg.c	0.63947	1.23Mb	48	0	$z \neq NULL \wedge ls(c, z) * ls(z, NULL),$ $z \neq w \wedge ls(c, z) * ls(z, w) * w \mapsto NULL,$ $z \neq w \wedge w \neq NULL \wedge ls(c, z) * ls(z, w) * w \mapsto w,$ $z \neq c \wedge c \mapsto NULL,$ $z \neq c \wedge z \neq c \wedge c \mapsto c * ls(c, NULL),$ $c = NULL \wedge emp$
find.c	0.05659	0.74Mb	12	0	$ls(c, b) * b \mapsto NULL,$ $b \neq NULL \wedge ls(c, b) * b \mapsto b,$ $b \neq c \wedge b \neq c \wedge c \mapsto c * lseg(c, NULL),$ $b \neq c \wedge c \mapsto NULL,$ $c = NULL \wedge emp$
insert.c	0.17049	0.74Mb	10	0	$e1 \neq NULL \wedge e2 \neq NULL \wedge c \neq d \wedge c \mapsto c * ls(c, d) * d \mapsto dta : e3,$ $e1 \neq NULL \wedge e2 \neq NULL \wedge c \neq NULL \wedge c \mapsto c * ls(c, NULL),$ $e1 \neq NULL \wedge c \mapsto NULL,$ $e1 \neq NULL \wedge e2 = NULL \wedge c \mapsto c * c \mapsto -,$ $e1 = NULL \wedge c \mapsto -,$ $c = NULL \wedge emp$
merge.c	0.56092	1.47Mb	30	30	—
reverse.c	0.01965	0.74Mb	4	0	$ls(c, NULL)$
traverse-circ.c	0.01322	0.49Mb	3	0	$c \mapsto c * ls(c, c)$

Program	Time (s)	Memory	# of Disjuncts	Unsafe Pre
t1394Diag-CancelIrp.c	0.08928	1.23Mb	11	2
t1394Diag-CancelIrpFix.c	0.20461	1.23Mb	10	0
t1394Diag_PnpRemoveDevice	T/O	—	—	—
t1394-BusResetRoutine.c	0.14924	1.23Mb	4	0
t1394-GetAddressData.c	0.08692	1.23Mb	9	2
t1394-GetAddressDataFix.c	0.08906	1.23Mb	3	0
t1394-IsochDetachCompletionRoutine.c	1.76640	2.70Mb	39	0
t1394-SetAddressData.c	0.06614	1.23Mb	9	1
t1394-SetAddressDataFix.c	0.12242	1.23Mb	9	0

Table 2. Experimental results from firewire device driver routines.

Stop