Large Spurious Cycles in Global Static Analyses and Their Algorithmic Mitigation

Hakjoo Oh
School of Computer Science and Engineering
Seoul National University

Abstract. We present a simple algorithmic extension of the classical call-strings approach to mitigate substantial performance degradation caused by spurious interprocedural cycles. Spurious interprocedural cycles are, in a realistic setting, key reasons for why approximate call-return semantics in both context-sensitive and -insensitive static analysis can make the analysis much slower than expected.

In the traditional call-strings-based context-sensitive static analysis, because the number of distinguished contexts must be finite, multiple call-contexts are inevitably joined at the entry of a procedure and the output at the exit is propagated to multiple return-sites. We found that these multiple returns frequently create a single large cycle (we call it “butterfly cycle”) covering almost all parts of the program and such a spurious cycle makes analyses very slow and inaccurate.

Our simple algorithmic technique (within the fixpoint iteration algorithm) identifies and prunes these spurious interprocedural flows. The technique’s effectiveness is proven by experiments with a realistic C analyzer to reduce the analysis time by 7%-96%. Since the technique is algorithmic, it can be easily applicable to existing analyses without changing the underlying abstract semantics, it is orthogonal to the underlying abstract semantics’ context-sensitivity, and its correctness is obvious.

1 Introduction

In a global semantic-based static analysis, it is inevitable to follow some spurious (unrealizable or invalid) return paths. Even though the underlying abstract semantics is context-sensitive, because the number of distinguished contexts must be finite, multiple call-contexts are joined at the entry of a procedure and the output at the exit are propagated to multiple return-sites. For example, in a conventional way of avoiding invalid return paths by distinguishing a finite \( k \geq 0 \) call-sites to each procedure, the analysis is doomed to still follow spurious paths if the input program’s nested call-depth is larger than the \( k \). Increasing the \( k \) to remove more spurious paths quickly hits a limit in practice because of the increasing analysis cost in memory and time.

In this article we present the following:

– in a realistic setting, these multiple returns often create a single large flow cycle (we call it “butterfly cycle”) covering almost all parts of the program,
such big spurious cycles make the conventional call-strings method that distinguishes the last $k$ call-sites [16] very slow and inaccurate,
this performance problem can be relieved by a simple extension of the call-strings method,
our extension is an algorithmic technique within the worklist-based fixpoint iteration routine, without redesigning the underlying abstract semantics, and
the algorithmic technique works regardless of the underlying abstract semantics’ context-sensitivity. The technique consistently saves the analysis time, without sacrificing (or with even improving) the analysis precision.

1.1 Problem: Large Performance Degradation By Inevitable, Spurious Interprocedural Cycles

Static analysis’ inevitable spurious paths make spurious cycles across procedure boundaries in global analysis. For example, consider the semantic equations in Fig. 1 that (context-insensitively ($k > 0$)) abstracts two consecutive calls to a procedure. The system of equations says to evaluate equation (4) and (6) for every return-site after analyzing the called procedure body (equation (3)). Thus, solving the equations follows a cycle: (2) → (3) → (4) → (5) → (2) → ...

Such spurious cycles degrade the analysis performance both in precision and speed. Spurious cycles exacerbate the analysis imprecision because they model spurious information flow. Spurious cycles degrade the analysis speed too because solving cyclic equations is repeatedly applying the equations in vain until a fixpoint is reached.

The performance degradation becomes dramatic when the involved interprocedural spurious cycles cover a large part of the input program. This is indeed the case in reality. In analyzing real C programs, we observed that the analysis follows (Section 2) a single large cycle that spans almost all parts of the input program. Such spurious cycle’s size can also be estimated by just measuring the strongly connected components (scc) in the “lexical” control flow graphs. Table 1 shows the sizes of the largest scc in some open-source programs. In most programs, such cycles cover most (80-90%) parts of the programs. Hence, globally analyzing a program is likely to compute a fixpoint of a function that describes almost all parts of the input program. Even when we do context-sensitive analysis ($k > 0$), large spurious cycles are likely to remain (Section 2).

1.2 Solution: An Algorithmic Mitigation Without Redesigning Abstract Semantics

We present a simple algorithmic technique inside a worklist-based fixpoint iteration procedure that, without redesigning the abstract semantics part, can

---

1 One node per lexical entity, ignoring function pointers.
2 We measured the sizes of all possible cycles in the flow graphs. Note that interprocedural cycles happen because of either spurious returns or recursive calls. Because recursive calls in the test C programs are immediate or spans only a small number of procedures, large interprocedural cycles are likely to be spurious ones.
effectively relieve the performance degradation caused by spurious interprocedural cycles in both context-sensitive \((k > 0)\) and -insensitive \((k = 0)\) analysis.

While solving flow equations, the algorithmic technique simply forces procedures to return to their corresponding called site, in order not to follow the last edge (edge \((3) \rightarrow (4)\) in Fig. 1) of the “butterfly” cycles. In order to enforce this, we control the equation-solving orders so that each called procedure is analyzed exclusively for its one particular call-site. To be safe, we apply our algorithm to only non-recursive procedures.

Consider the equation system in Fig. 1 again and think of a middle of the analysis (equation-solving) sequence, ... \(\rightarrow (5) \rightarrow (2) \rightarrow (3)\), which indicates that the analysis of procedure \(f\) is invoked from \((5)\) and is now finished. After the evaluation of \((3)\), a classical worklist algorithm inserts all the equations, \((4)\) and \((6)\), that depend on \((3)\). But, if we remember the fact that \(f\) has been invoked from \((5)\) and the other call-site \((1)\) has not invoked the procedure until the analysis of \(f\) finishes, we can know that continuing with \((4)\) is useless, because the current analysis of \(f\) is only related to \((5)\), but not to other calls like \((1)\). So, we process only \((6)\), pruning the spurious sequence \((3) \rightarrow (4) \rightarrow \ldots\).

We integrated the algorithm inside an industrialized abstract-interpretation-based C static analyzer \([6, 7]\) and measured performance gains derived from avoiding spurious cycles. We have saved 7%-96% of the analysis time for context-insensitive or -sensitive global analysis for open-source benchmarks.

1.3 Contributions

- We present a simple extension of the classical call-strings approach, which effectively reduces the inefficiency caused by large, inevitable, spurious interprocedural cycles.

We prove the effectiveness of the technique by experiments with an industrial-strength C static analyzer \([6, 7]\) in globally analyzing medium-scale open-source programs.
Table 1. The sizes of the largest strongly-connected components in the “lexical” control flow graphs of real C programs. In most cases, most procedures and nodes in program belong to a single cycle.

<table>
<thead>
<tr>
<th>Program</th>
<th>Procedures in the largest cycle</th>
<th>Basic-blocks in the largest cycle</th>
</tr>
</thead>
<tbody>
<tr>
<td>spell-1.0</td>
<td>24/31 (77%)</td>
<td>751/782 (95%)</td>
</tr>
<tr>
<td>gzip-1.2.4a</td>
<td>100/135 (74%)</td>
<td>5,988/6,271 (95%)</td>
</tr>
<tr>
<td>sed-4.0.8</td>
<td>230/294 (78%)</td>
<td>14,559/14,976 (97%)</td>
</tr>
<tr>
<td>tar-1.13</td>
<td>205/222 (92%)</td>
<td>10,194/10,800 (94%)</td>
</tr>
<tr>
<td>wget-1.9</td>
<td>346/434 (80%)</td>
<td>15,249/16,544 (92%)</td>
</tr>
<tr>
<td>bison-1.875</td>
<td>410/832 (49%)</td>
<td>12,558/18,110 (69%)</td>
</tr>
<tr>
<td>proftpd-1.3.1</td>
<td>910/1,096 (85%)</td>
<td>35,386/41,062 (86%)</td>
</tr>
</tbody>
</table>

– The technique is meaningful in two ways. Firstly, the technique aims to alleviate one major reason (spurious interprocedural cycles) for substantial inefficiency in global static analysis. Secondly, it is purely an algorithmic technique inside the worklist-based fixpoint iteration routine. So, it can be directly applicable without changing the analysis’ underlying abstract semantics, regardless of whether the semantics is context-sensitive or not. The technique’s correctness is obvious enough to avoid the burden of a safety proof that would be needed if we newly designed the abstract semantics.

– We report one key reason (spurious interprocedural cycles) for why less accurate context-sensitivity actually makes the analyses very slow. Though it is well-known folklore that less precise analysis does not always have less cost [11, 13, 15], there haven’t been realistic experiments about the explicit reason.

1.4 Related Work

We compare our method with other approaches that eliminate invalid paths on the basis of their applicability to general semantic-based static analyzers.\(^3\) The classical call-strings approach that retains the last \(k\) call-sites [16] is popular in practice but its precision is not enough to mitigate large spurious cycles. This \(k\)-limiting method is widely used in practice [1, 10, 11] and actually it is one of very few options available for semantic-based global static analysis with infinite domains and non-distributive flow functions (e.g., [1, 7]). Though it removes some invalid paths, it induces a large spurious cycle because it permits multiple returns of procedures. Our algorithm is an extension of the \(k\)-limiting method and adds extra precision that relieves the performance problem.

Another approximate call-strings method that uses full context-sensitivity for non-recursive procedures and treats recursive call cycles as gotos is practical

\(^3\) For example, such analyzers include octagon-based analyzers (e.g., [2]), interval-based analyzers (e.g., [6, 7]), value set analysis [1], and program analyzer generators (e.g., [10]), which usually use infinite (height) domains and non-distributive flow functions.
for points-to analysis [17, 18] but too costly for more general semantic-based
analysis. Though these approaches are more precise than \( k \)-limiting method,
it is unknown whether the BDD-based method [18] or regular-reachability [17]
are also applicable in practice to semantic-based analyzers rather than pointer
analysis. Our algorithm can be useful for analyses for which these approaches
hit a limit in practice and \( k \)-limiting is required.

Full call-strings approaches [16, 8, 9] and functional approaches [16] do not
suffer from spurious cycles but are limited to restricted classes of data flow anal-
ysis problems. The original full call-strings method [16] prescribes the domain to
be finite and its improved algorithms [8, 9] are also limited to bit-vector problems
or finite domains. Khedker et al.’s algorithm [9] supports infinite domains only
for demand-driven analysis. The purely functional approach [16] requires comp-
act representations of flow functions. The iterative (functional) approach [16]
requires the domain to be finite.

Reps et al.’s algorithms [12, 14] to avoid unrealizable paths are limited to
analysis problems that can be expressed only in their graph reachability frame-
work. their algorithm cannot handle prevalent yet non-distributive analyses. For
example, our analyzer that uses the interval domain [5] with non-distributive
flow functions does not fall into either their IFDS [12] or IDE [14] problems.
Meanwhile, our algorithm is independent of the underlying abstract semantic
functions. The regular-reachability [17], which is a restricted version of Reps et
al.’s, also requires the analysis problem to be expressed in graph reachability
problem.

Chamber et al.’s technique [4] is similar to ours but entails a relatively large
change to an existing worklist order. Their technique analyzes each procedure
intraprocedurally, and at call-sites continues the analysis of the callee. It returns
to analyze the nodes of the caller only after finishing the analysis of the callee.
Our worklist prioritizes the callee only over the call nodes that invoke the callee,
not all the nodes of the caller, which is a relatively smaller change than Chamber
et al.’s. In addition, they assume worst case results for recursive calls, but we
does not degrade the analysis precision for recursive calls.

2 Performance Problems due to Large Spurious Cycles

If a spurious cycle is created by multiple calls to a procedure \( f \), then all the
procedures that are reachable from \( f \) or that reach \( f \) via the call-graph belong
to the cycle because of call and return flows. For example, consider a call-chain
\( \cdots f_1 \rightarrow f_2 \cdots \). If \( f_1 \) calls \( f_2 \) multiple times, creating a spurious butterfly cycle
\( f_1 \bowtie f_2 \) between them, then fixpoint-solving the cycle involves all the nodes of
procedures that reach \( f_1 \) or that are reachable from \( f_2 \). This situation is common
in C programs. For example, in GNU software, the \texttt{xmalloc} procedure, which is
in charge of memory allocation, is called from many other procedures, and hence
generates a butterfly cycle. Then every procedure that reaches \texttt{xmalloc} via the
call-graph is trapped into a fixpoint cycle.
Fig. 2. Analysis localities. Because of butterfly cycles, similar patterns are repeated several times during the analysis and each pattern contains almost all parts of the programs.

In conventional context-sensitive analysis that distinguishes the last \( k \) call-sites [16], if there are call-chains of length \( l (> k) \) in programs, it’s still possible to have a spurious cycle created during the first \( l - k \) calls. This spurious cycle traps the last \( k \) procedures into a fixpoint cycle by the above reason.

One spurious cycle in real C programs traps as many as 80-90% of basic blocks of the program into a fixpoint cycle. Fig. 2 shows this phenomenon. In the figures, the x-axis represents the execution time of the analysis and the y-axis represents the procedure name, which is mapped to unique integers. During the analysis, we draw the graph by plotting the point \((t, f)\) if the analysis’ worklist algorithm visits a node of procedure \( f \) at the time \( t \). For brevity, the graph for sed-4.0.8 is shown only up to 100,000 iterations among more than 3,000,000 total iterations. From the results, we first observe that similar patterns are repeated and each pattern contains almost all procedures in the program. And we find that there are much more repetitions in the case of a large program (sed-4.0.8, 26,807 LOC) than a small one (spell-1.0, 2,213 LOC): more than 150 repeated iterations were required to analyze sed-4.0.8 whereas spell-1.0 needed about 30 repetitions.

3 Our Algorithmic Mitigation Technique

Our technique is a simple addition to the existing worklist-based fixpoint algorithm to avoid spurious interprocedural returns. The technique does not depend on the underlying abstract semantics.

We first describe the traditional call-strings-based analysis algorithm (section 3.2) as well as the representation of programs (section 3.1). Then we present our algorithmic extension of the classical algorithm (section 3.3).
3.1 Graph Representation of Programs

We assume that a program is represented by a supergraph \([12]\). A supergraph consists of control flow graphs of procedures with interprocedural edges connecting each call-site to its callee. Each node \(n \in \text{Node}\) in the graph has one of the five types:

\[
\text{entry}_f \mid \text{exit}_f \mid \text{call}_g,r_f \mid \text{rtn}_c_f \mid \text{cmd}_f
\]

The subscript \(f\) of each node represents the procedure name enclosing the node. \(\text{entry}_f\) and \(\text{exit}_f\) are entry and exit nodes of procedure \(f\). A call-site in a program is represented by a call node and its corresponding return node. A call node \(\text{call}_g,r_f\) indicates that it invokes a procedure \(g\) and its corresponding return node is \(r\). We assume that function pointers are resolved (before the analysis). Node \(\text{rtn}_c_f\) represents a return node in \(f\) whose corresponding call node is \(c\). Node \(\text{cmd}_f\) represents a general command statement. Edges are compiled by a function, \(\text{succof}\), which maps each node to its successors. \(\text{CallNode}\) is the set of call nodes in a program.

3.2 Normal\(_k\): A Normal Call-Strings-Based Analysis Algorithm

Call-strings are sequences of call nodes. To make them finite, we only consider call-strings of length at most \(k\) for some fixed integer \(k \geq 0\). We write \(\text{CallNode}^{\leq k} = \Delta\) for the set of call-strings of length \(\leq k\). We write \([c_1,c_2,\ldots,c_i]\) for a call-string of call sequence \(c_1,c_2,\ldots,c_i\). Given a call-string \(\delta\) and a call node \(c\), \([\delta,c]\) denotes a call-string obtained by appending \(c\) to \(\delta\). In the case of context-insensitive analysis (\(k = 0\)), we use \(\Delta = \{\epsilon\}\), where the empty call-string \(\epsilon\) means no context-information.

Fig. 3.(a) shows the worklist-based fixpoint iteration algorithm that performs call-strings(\(\Delta\))-based context-sensitive (or insensitive, when \(k = 0\)) analysis. The algorithm computes a table \(T \in \text{Node} \rightarrow \text{State}\) which associates each node with its input state \(\text{State} = \Delta \rightarrow \text{Mem}\), where \(\text{Mem}\) denotes abstract memory, which is a map from program variables to abstract values. That is, call-strings are tagged to the abstract memories and are used to distinguish the memories propagated along different interprocedural paths, to a limited extent (the last \(k\) call-sites).

The worklist \(W\) consists of node and call-string pairs. The algorithm chooses a work-item \((n,\delta) \in \text{Node} \times \Delta\) from the worklist and evaluate the node \(n\) with the flow function \(\hat{F}\). Next work-items to be inserted into the worklist are defined by the function \(N \in \text{Node} \times \Delta \rightarrow 2^{\text{Node} \times \Delta}\):

\[
N(n,\delta) = \begin{cases} 
\{ (r,\delta') \mid \delta = [\delta',\text{call}_f^{g,r}]_k \land \delta' \in \text{dom}(T(\text{call}_f^{g,r})) \} & \text{if } n = \text{exit}_g \\
\{ (\text{entry}_g, [\delta,n]) \} & \text{if } n = \text{call}_f^{g,r} \\
\{ (n',\delta) \mid n' \in \text{succof}(n) \} & \text{otherwise}
\end{cases}
\]

where \(\text{dom}(f)\) denotes the domain of map \(f\) and \([\delta,c]_k\) denotes the call-string \([\delta,c]\) but possibly truncated so as to keep at most the last \(k\) call-sites.

The algorithm can follow spurious return paths if the input program’s nested call-depth is larger than the \(k\). The mapping \(\delta'\) to \([\delta',\text{call}_f^{g,r}]_k\) is not one-to-one.
and $\mathcal{N}$ possibly returns many work-items at an exit node. The following example illustrates this situation.

**Example 1.** Let $k = 2$ and suppose call-strings $[c_1, c_3]$ and $[c_2, c_3]$ are tagged to a call node $call_{f}^{g,r}$. Suppose $call_{f}^{g,r}$ calls $g$ under the call-string $[c_1, c_3]$. By the definition of $\mathcal{N}$, the call-string at $entry_g$ is $[c_1, c_3, call_{f}^{g,r}]_2 = [c_3, call_{f}^{g,r}]$. After the analysis of $g$, the call-string at $exit_g$ is also $[c_3, call_{f}^{g,r}]$. When $g$ returns, since the call-string at $exit_g$ equals to $[c_1, c_3, call_{f}^{g,r}]_2$ and $[c_2, c_3, call_{f}^{g,r}]_2$, $\mathcal{N}$ returns two work-items $(r, [1, 3])$ and $(r, [2, 3])$.

We call the algorithm $\text{Normal}_k$ ($k = 0, 1, 2, \ldots$). $\text{Normal}_0$ performs context-insensitive analysis, $\text{Normal}_1$ performs context-sensitive analysis that distinguishes the last 1 call-site, and so on.

### 3.3 $\text{Normal}_k$/RSS: Our Algorithm

**Definition 1.** When a procedure $g$ is called from a call node $call_{f}^{g,r}$ under context $\delta$, we say that $(call_{f}^{g,r}, \delta)$ is the call-context for that procedure call. Since each call node $call_{f}^{g,r}$ has a unique return node, we interchangeably write $(r, \delta)$ and $(call_{f}^{g,r}, \delta)$ for the same call-context.

Our return-site-sensitive (RSS) technique is simple. When calling a procedure at a call-site, the call-context for that call is remembered until the procedure returns. The bookkeeping cost is limited to only one memory entry per procedure. This is possible by the following strategies:

1. **Single return:** Whenever the analysis of a procedure $g$ is started from a call node $call_{f}^{g,r}$ in $f$ under call-string $\delta$, the algorithm remembers its call-context $(r, \delta)$, consisting of the corresponding return node $r$ and the call-string $\delta$. And upon finishing analyzing $g$’s body, after evaluating $exit_g$, the algorithm inserts only the remembered return node and its call-string $(r, \delta)$ into the worklist. Multiple returns are avoided. For correctness, this single return should be allowed only when other call nodes that call $g$ are not analyzed until the analysis of $g$ from $(call_{f}^{g,r}, \delta)$ completes.

2. **One call per procedure, exclusively:** We implement the single return policy by using one memory entry per procedure to remember the call-context. This is possible if we can analyze each called procedure exclusively for its one particular call-context. If a procedure is being analyzed from a call node $c$ with a call-string $\delta$, processing all the other calls that call the same procedure should wait until the analysis of the procedure from $(c, \delta)$ is completely finished. This one-exclusive-call-per-procedure policy is enforced by not selecting from the worklist other call nodes that (directly or transitively) call the procedures that are currently being analyzed.

3. **Recursion handling:** The algorithm gives up the single return policy for recursive procedures. This is because we cannot finish analyzing recursive procedure body without considering another calls (recursive calls) in it. Recursive procedures are handled in the same way as the normal worklist algorithm.
The algorithm does not follow spurious return paths regardless of the program’s nested call-depth. While Normal\(_k\) starts losing its power when a call chain’s length is larger than \(k\), Normal\(_k\)/RSS does not. The following example shows this difference between Normal\(_k\) and Normal\(_k\)/RSS.

**Example 2.** Consider a program that has the following call-chain (where \(f_1 \xrightarrow{c_1,c_2} f_2\) denotes that \(f_1\) calls \(f_2\) at call-sites \(c_1\) and \(c_2\)) and suppose \(k = 1\):

\[
f_1 \xrightarrow{c_1,c_2} f_2 \xrightarrow{c_3,c_4} f_3
\]

- Normal\(_1\): The analysis results for \(f_2\) are distinguished by \([c_1]\) and \([c_2]\) hence no butterfly cycle happens between \(f_1\) and \(f_2\). Now, when \(f_3\) is called from \(f_2\) at \(c_3\), we have two call-contexts \((c_3,[c_1])\) and \((c_3,[c_2])\) but analyzing \(f_3\) proceeds with context \([c_3]\) (because \(k = 1\)). That is, Normal\(_k\) forgets the call-context for procedure \(f_3\). Thus the result of analyzing \(f_3\) must flow back to all call-contexts with return site \(c_3\), i.e., to both the call-contexts \((c_3,[c_1])\) and \((c_3,[c_2])\).
- Normal\(_1\)/RSS: The results for \(f_2\) and \(f_3\) are distinguished in the same way as Normal\(_1\). But, Normal\(_1\)/RSS additionally remembers the call-contexts for every procedure call. If \(f_3\) was called from \(c_3\) under context \([c_1]\), our algorithmic technique forces Normal\(_k\) to remember the call-context \((c_3,[c_1])\) for that procedure call. And finishing analyzing \(f_3\)’s body, \(f_3\) returns only to the remembered call-context \((c_3,[c_1])\). This is possible by the one-exclusive-call-per-procedure policy.

We ensure the one-exclusive-call-per-procedure policy by prioritizing a callee over call-sites that (directly or transitively) invoke the callee. The algorithm always analyzes the nodes of the callee \(g\) first prior to any other call nodes that invoke \(g\); before selecting a work-item as a next job, we exclude from the worklist every call node \(call^g_r\) to \(g\) if the worklist contains any node of procedure \(h\) that can be reached from \(g\) along some call-chains \(g \rightarrow \cdots \rightarrow h\), including the case of \(g = h\). After excluding such call nodes, the algorithm chooses a work-item in the same way as a normal worklist algorithm.

**Example 3.** Consider a worklist \(\{(call^g_{r1}, \delta_1), (call^h_{r2}, \delta_2), (n_h, \delta_3), (call^h_{r4}, \delta_4)\}\) and assume there is a path \(f \rightarrow g \rightarrow h\) in call graph. When choosing a work-item from the worklist, our algorithm first excludes all the call nodes that invoke procedures now being analyzed: \(call^h_{r2}\) is excluded because \(h\)’s node \(n_h\) is in the worklist. Similarly, \(call^g_{r1}\) is excluded because there is a call-chain \(g \rightarrow h\) in call graph and \(h\)’s node \(n_h\) exists. So, the algorithm chooses a work-item from \(\{(n_h, \delta_3), (call^h_{r4}, \delta_4)\}\). The excluded work-items \((call^g_{r1}, \delta_1)\) and \((call^h_{r2}, \delta_2)\) will not be selected unless there are no nodes of \(h\) in the worklist.

Fig. 3(b) shows our algorithmic technique that is applied to the normal worklist algorithm of Fig. 3(a). To transform Normal\(_k\) into Normal\(_k\)/RSS, only shaded lines are inserted; other parts remain the same. ReturnSite is a map to record a single return site information (return node and context pair) per procedure.
Lines 15-16 are for remembering a single return when encountering a call-site. The algorithm checks if the current node is a call-node and its target procedure is non-recursive (the recursive predicate decides whether the procedure is recursive or not), and if so, it remembers its single return-site information for the callee. Lines 17-22 handle procedure returns. If the current node is an exit of a non-recursive procedure, only the remembered return for that procedure is used as a next work-item, instead of all possible next (successor, context) pairs (line 23). Prioritizing callee over call nodes is implemented by delaying call nodes to procedures now being analyzed. To do this, in line 12-13, the algorithm excludes the call nodes \( \{(call_g, \_), (nh, \_) \in W | (nh, \_) \in W \land \text{reach}(g, h) \land \neg \text{recursive}(g) \} \) that invoke non-recursive procedures whose nodes are already contained in the current worklist. \( \text{reach}(g, h) \) is true if there is a path in call graph from \( g \) to \( h \).

**Example 4.** Analyzing the program in the left-hand side of Fig. 4 proceeds as shown in the right-hand side table. (Assume that \( k = 0 \), the choose function in Fig. 3 arbitrarily chooses an element from the given worklist, and the initial worklist is \( \{1, 4\} \).) For each iteration of the algorithm, the table shows the contents of the current worklist \( (W) \), call nodes that are excluded at this iteration \( (S) \), return site information \( (\text{ReturnSite}) \), and the updated worklist \( (W) \). \( \bar{n} \) represents the chosen node for each iteration. When the algorithm processes call node 1 at the first iteration, \( f \) remembers its corresponding return-site 4. At the 3rd and 4th iterations, node 5 was excluded, because it is another call to \( f \) and the worklist contains the nodes of \( f \) at both iterations. At the exit of \( f \) (when processing node 3 at the 4th iteration), only \( \text{ReturnSite}(f) = 4 \) is inserted into the worklist instead of \( \text{succof}(f) = \{4, 6\} \).

**Correctness & Precision** One noticeable thing is that the result of our algorithm is not a fixpoint of the given flow equation system, but still a sound approximation of the program semantics. Since the algorithm prunes some computation steps during worklist algorithm (at exit nodes of non-recursive procedures), the result of the algorithm may not be a fixpoint of the original equation system. However, because the algorithm prunes only spurious returns that definitely do not happen in the real executions of the program, our algorithm does not miss any real executions.

For any \( f \) and any arbitrary call-context \( (call_{g, r}, \delta) \), the single return to \( (r, \delta) \) after analyzing \( f \) is correct if the state from \( (call_{g, r}, \delta) \) is implied by the input state used in the analysis of \( f \) and its result is guaranteed to be returned to \( (r, \delta) \). The state from every call-context flows into \( f \) (abstract semantics). Our single-return policy does not miss returning \( f \)'s analysis result to its corresponding call-context\(^4\) because (1) we remember the context at each call; (2) for every different call, modulo the underlying context-sensitivity, we exclusively analyze

\(^4\) Here, we ignore the cases where the callee never returns (e.g., it calls exit()). However, even though that happens, we can enforce the return of callee by always inserting the exit node of a procedure when inserting the entry node of the procedure into the worklist.
Title Suppressed Due to Excessive Length

(a) a normal worklist algorithm Normal_k (b) our algorithm Normal_k/RSS

Fig. 3. A normal context-sensitive worklist algorithm Normal_k and its RSS modification Normal_k/RSS. The left-hand side shows a worklist algorithm for call-strings based context-sensitive analysis. The right-hand side shows the RSS algorithm for the same analysis. These two algorithms are the same except for shaded regions. For brevity, we omit the usual definition of $F$, which updates the worklist in addition to computing the flow equation’s body.

Fig. 4. A running example
Because we cannot enforce this exclusivity for recursive calls, we do not apply the algorithm to recursive procedures.

Normal$_k$/RSS is always at least as precise as Normal$_k$. Because Normal$_k$/RSS prunes some (worklist-level) computations that occur along invalid return paths, it is likely to have an effect of avoiding propagations of values along invalid return paths. The precision of Normal$_k$/RSS varies depending on the worklist order, but is no worse than that of Normal$_k$.

**Example 5.** Consider the program in Fig. 4 again, and suppose the current worklist is \{1, 5\}. When analyzing the program with Normal$_0$, the fixpoint-solving follows both spurious return paths, regardless of the worklist order,

\begin{align*}
1 & \rightarrow 2 \rightarrow 3 \rightarrow 6 \\
5 & \rightarrow 2 \rightarrow 3 \rightarrow 4
\end{align*}

because of multiple returns from node 3. When analyzing with Normal$_0$/RSS, there are two possibilities, depending on the worklist order:

1. When Normal$_0$/RSS selects node 1 first: Then the fixpoint iteration sequence may be 1; 2; 3; 4; 5; 2; 3; 6. This sequence involves the spurious path (1) (because the second visit to node 2 uses the information from node 1 as well as from node 5), but not (2). Normal$_0$/RSS is more precise than Normal$_0$.

2. When Normal$_0$/RSS selects node 5 first: Then the fixpoint iteration sequence may be 5; 2; 3; 6; 1; 2; 3; 4; 5; 2; 3; 6. This computation involves both spurious paths (1) and (2). With this iteration order, Normal$_0$ and Normal$_0$/RSS have the same precision.

## 4 Experiments

We implemented our algorithm inside a realistic C analyzer and experiments with open-source programs show that Normal$_k$/RSS for any $k$ is very likely faster than Normal$_k$, and that even Normal$_{k+1}$/RSS can be faster than Normal$_k$.

### 4.1 Setting Up

Normal$_k$ is our underlying worklist algorithm, on top of which our industrialized static analyzer [6, 7] for C is installed. The analyzer is an interval-domain-based abstract interpreter. The analyzer performs by default flow-sensitive and call-string-based context-sensitive global analysis on the supergraph of the input programs; it computes $T = \text{Node} \rightarrow \text{State}$ where $\text{State} = \Delta \rightarrow \text{Mem}$. Mem denotes abstract memory $\text{Mem} = \text{Addr} \rightarrow \text{Val}$ where $\text{Addr}$ denotes abstract locations that are either program variables or allocation sites, and $\text{Val}$ denotes abstract values including $\hat{\mathbb{Z}}$ (interval domain), $2^{\text{Addr}}$ (points-to set), and $2^{\text{AllocSite} \times \hat{\mathbb{Z}} \times \hat{\mathbb{Z}}}$ (array block, consisting of base address, offset, and size [7]).

We measured the net effects of avoiding spurious interprocedural cycles. Since our algorithmic technique changes the existing worklist order, performance differences between Normal$_k$ and Normal$_k$/RSS could be attributed not only to
Table 2. Benchmark programs and their raw analysis results. Lines of code (LOC) are given before preprocessing. The number of nodes in the supergraph (#nodes) is given after preprocessing. \( k \) denotes the size of call-strings used for the analysis. Entries with \( \infty \) means missing data because of our analysis running out of memory.

<table>
<thead>
<tr>
<th>Program</th>
<th>LOC</th>
<th>#nodes</th>
<th>( k )-call-strings</th>
<th>#iterations</th>
<th>time</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Normal/RSS</td>
<td></td>
</tr>
<tr>
<td>spell-1.0</td>
<td>2,213</td>
<td>782</td>
<td>0</td>
<td>31,864/5,800</td>
<td>60.98</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>1</td>
<td>31,913/10,109</td>
<td>55.02</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>2</td>
<td>31,088/15,226</td>
<td>102.28</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>1</td>
<td>34,508/30,311</td>
<td>144.37</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>2</td>
<td>40,176/36,058</td>
<td>183.49</td>
</tr>
<tr>
<td>barcode-0.96</td>
<td>4,460</td>
<td>2,642</td>
<td>0</td>
<td>22,006/19,556</td>
<td>91.42</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>1</td>
<td>34,508/30,311</td>
<td>144.37</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>2</td>
<td>40,176/36,058</td>
<td>183.49</td>
</tr>
<tr>
<td>httptunnel-3.3</td>
<td>6,174</td>
<td>2,757</td>
<td>0</td>
<td>442,159/88,359</td>
<td>2020.10</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>1</td>
<td>267,291/116,666</td>
<td>1525.26</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>2</td>
<td>609,623/251,575</td>
<td>5983.27</td>
</tr>
<tr>
<td>httpd-3.3</td>
<td>10,900</td>
<td>9,298</td>
<td>0</td>
<td>3,452,228/230,300</td>
<td>3270.40</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>1</td>
<td>1,174,632/150,391</td>
<td>1116.25</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>2</td>
<td>40,176/36,058</td>
<td>183.49</td>
</tr>
<tr>
<td>gzip-1.2.4a</td>
<td>7,327</td>
<td>6,271</td>
<td>0</td>
<td>664,063/88,359</td>
<td>4601.23</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>1</td>
<td>991,135/116,666</td>
<td>1525.26</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>2</td>
<td>272,377/138,077</td>
<td>2445.56</td>
</tr>
<tr>
<td>httpd-3.3</td>
<td>9,344</td>
<td>5,147</td>
<td>0</td>
<td>1,174,632/150,391</td>
<td>1116.25</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>1</td>
<td>1,174,632/150,391</td>
<td>1116.25</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>2</td>
<td>40,176/36,058</td>
<td>183.49</td>
</tr>
<tr>
<td>parser</td>
<td></td>
<td>9,298</td>
<td>0</td>
<td>3,452,228/230,300</td>
<td>3270.40</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>1</td>
<td>991,135/116,666</td>
<td>1525.26</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>2</td>
<td>272,377/138,077</td>
<td>2445.56</td>
</tr>
<tr>
<td>bc-1.06</td>
<td>13,093</td>
<td>4,924</td>
<td>0</td>
<td>1,964,396/412,549</td>
<td>23515.27</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>1</td>
<td>3,452,228/230,300</td>
<td>3270.40</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>2</td>
<td>991,135/116,666</td>
<td>1525.26</td>
</tr>
<tr>
<td>less-290</td>
<td>18,449</td>
<td>7,754</td>
<td>0</td>
<td>3,452,228/230,300</td>
<td>3270.40</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>1</td>
<td>3,452,228/230,300</td>
<td>3270.40</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>2</td>
<td>991,135/116,666</td>
<td>1525.26</td>
</tr>
<tr>
<td>twolf</td>
<td>19,700</td>
<td>14,610</td>
<td>0</td>
<td>3,028,814/139,082</td>
<td>1395.32</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>1</td>
<td>3,028,814/139,082</td>
<td>1395.32</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>2</td>
<td>991,135/116,666</td>
<td>1525.26</td>
</tr>
<tr>
<td>tar-1.13</td>
<td>20,254</td>
<td>10,800</td>
<td>0</td>
<td>4,748,749/700,474</td>
<td>75013.88</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>1</td>
<td>3,452,228/230,300</td>
<td>3270.40</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>2</td>
<td>991,135/116,666</td>
<td>1525.26</td>
</tr>
<tr>
<td>make-3.76.1</td>
<td>27,304</td>
<td>11,001</td>
<td>0</td>
<td>4,614,352/2,511,582</td>
<td>44853.40</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>1</td>
<td>3,452,228/230,300</td>
<td>3270.40</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>2</td>
<td>991,135/116,666</td>
<td>1525.26</td>
</tr>
</tbody>
</table>

avoiding spurious cycles but also to the changed worklist order. In order to measure the net effects of avoiding spurious cycles, we applied the same worklist order to both Normal\(_k\) and Normal\(_k\)/RSS. To be specific, the order (between nodes) that we used is a reverse topological order between procedures on the call graph: a node \( n \) of a procedure \( f \) precedes a node \( m \) of a procedure \( g \) if \( f \) precedes \( g \) in the reverse topological order in the call graph. If \( f \) and \( g \) are the same procedure, the order between the nodes are defined by the weak topological order [3] on the control flow graph of the procedure. Note that this ordering itself contains the “prioritize callees over call-sites” feature and we don’t explicitly need the delaying call technique (lines 12-13 in Fig. 3(b)) in Normal\(_k\)/RSS. Hence the worklist order for Normal\(_k\) and Normal\(_k\)/RSS are the same.\(^5\)

We have analyzed 11 open-source software packages. Table 2 shows our benchmark programs as well as their raw analysis results. All experiments were done on a Linux 2.6 system running on a Pentium4 3.2 GHz box with 4 GB of main memory.

\(^5\) In fact, the order described here is the one our analyzer uses by default, which consistently shows better performance than naive worklist management scheme (BFS/DFS) or simple “wait-at-join” techniques (e.g., [7]).
4.2 Reduced Analysis Time

We use two performance measures: (1) \#iterations is the total number of iterations during the worklist algorithm. The number directly indicates the amount of computation; (2) time is the CPU time spent during the analysis.

Fig. 5 compares the analysis time between Normal_k/RSS and Normal_k for \( k = 0, 1, 2 \). In this comparison, Normal_k/RSS reduces the analysis time of Normal_k by 7%-96%.

– When \( k = 0 \) (context-insensitive) : Normal_0/RSS has reduced the analysis time by, on average, about 74% against Normal_0. For most programs, the analysis time has been reduced by more than 50%. There is one exception: barcode. The analysis time has been reduced by 9%. This is because barcode has unusual call structures: it does not call a procedure many times, but calls many different procedures one by one. So, the program contains few butterfly cycles.

– When \( k = 1 \) : Normal_1/RSS has reduced the analysis time by, on average, about 60% against Normal_1. Compared to the context-insensitive case, for all programs, cost reduction ratios have been slightly decreased. As an example, for spell, the reduction ratio when \( k = 0 \) is 86% and the ratio when \( k = 1 \) is 76%. This is mainly because, in our analysis, Normal_0 costs more than Normal_1 for most programs (spell, httptunnel, proxyknife, jwhois). For httptunnel, in Table 2, the analysis time (2020.10 s) for \( k = 1 \) is less than the time (1525.26 s) for \( k = 0 \). This means that performance problems by butterfly cycles is much severe when \( k = 0 \) than that of \( k = 1 \), because by increasing context-sensitivity some spurious paths can be removed. However, by using our algorithm, we can still reduce the cost of Normal_1 by 60%.

– When \( k = 2 \) : Normal_2/RSS has reduced the analysis time by, on average, 69% against Normal_2. Compared to the case of \( k = 1 \), the cost reduction ratio has been slightly increased for most programs. For example, the ratio for spell has changed from 76% to 81%. In the analysis of Normal_2, since the equation system is much larger than that of Normal_1, our conjecture is that the size of butterfly cycles is likely to get larger. Since larger butterfly cycles causes more serious problems (Section 2), our RSS algorithm is likely to greatly reduce useless computation.

Fig. 6 compares the performance of Normal_{k+1}/RSS against Normal_k for \( k = 0, 1 \). The result shows that, for all programs except barcode, even Normal_{k+1}/RSS is faster than Normal_k. Since Normal_{k+1}/RSS can be even faster than Normal_k, if memory cost permits, we can consider using Normal_{k+1}/RSS instead of Normal_k.

4.3 Increased Analysis Precision

Table 3 compares the precision between Normal_0 and Normal_0/RSS.\(^6\) In order to measure the increased precision, we first joined all the memories associated with

\(^6\) We compared the precision for the case of \( k = 0 \) and for the first five programs in Table 2 because we need more memory to do the precision comparison (we should keep two analysis results of Normal_0 and Normal_0/RSS at the same time).
each program point (Node). Then we counted the number of constant intervals (#const, e.g., [1, 1]), finite intervals (#finite, e.g., [1, 5]), intervals with one infinity (#open, e.g., [−1, +∞) or (−∞, 1]), and intervals with two infinity (#top, (−∞, +∞)) from interval values (ˆZ) and array blocks (2^AllocSite × 2 × 2) contained in the joined memory. The constant interval and top interval indicate the most precise and imprecise values, respectively. The results show that Normal_0/RSS is more precise (spell, barcode, httptunnel, gzip) than Normal_0 or the precision is the same (jwhois).

5 Conclusion

We have presented a simple algorithmic technique to alleviate substantial inefficiency in global static analysis caused by large spurious interprocedural cycles. Such cycles are identified as a major reason for the folklore problem in static analysis that less precise analyses sometimes are slower. Although this inefficiency might not come to the fore when analyzing small programs, globally analyzing medium or large programs makes it outstanding. The proposed algorithmic technique reduces the analysis time by 7%-96% for open-source benchmarks.

Though tuning the precision of static analysis can in principle be controlled solely by redesigning the underlying abstract semantics, our algorithmic tech-
Fig. 6. Comparison of time between Normal_k and Normal_{k+1}/RSS, for k = 0, 1. For most programs except barcode, Normal_{k+1}/RSS is faster than Normal_k.

Table 3. Comparison of precision between Normal_0 and Normal_0/RSS.

<table>
<thead>
<tr>
<th>Program</th>
<th>Analysis</th>
<th>#const</th>
<th>#finite</th>
<th>#open</th>
<th>#top</th>
</tr>
</thead>
<tbody>
<tr>
<td>spell-1.0</td>
<td>Normal_0</td>
<td>345</td>
<td>88</td>
<td>33</td>
<td>143</td>
</tr>
<tr>
<td></td>
<td>Normal_0/RSS</td>
<td>345</td>
<td>89</td>
<td>35</td>
<td>140</td>
</tr>
<tr>
<td>barcode-0.96</td>
<td>Normal_0</td>
<td>2136</td>
<td>588</td>
<td>240</td>
<td>527</td>
</tr>
<tr>
<td></td>
<td>Normal_0/RSS</td>
<td>2136</td>
<td>589</td>
<td>240</td>
<td>526</td>
</tr>
<tr>
<td>httptunnel-3.3</td>
<td>Normal_0</td>
<td>1337</td>
<td>342</td>
<td>120</td>
<td>481</td>
</tr>
<tr>
<td></td>
<td>Normal_0/RSS</td>
<td>1345</td>
<td>342</td>
<td>120</td>
<td>473</td>
</tr>
<tr>
<td>gzip-1.2.4a</td>
<td>Normal_0</td>
<td>1995</td>
<td>714</td>
<td>255</td>
<td>1214</td>
</tr>
<tr>
<td></td>
<td>Normal_0/RSS</td>
<td>1995</td>
<td>716</td>
<td>255</td>
<td>1212</td>
</tr>
<tr>
<td>jwhois-3.0.1</td>
<td>Normal_0</td>
<td>2740</td>
<td>415</td>
<td>961</td>
<td>1036</td>
</tr>
<tr>
<td></td>
<td>Normal_0/RSS</td>
<td>2740</td>
<td>415</td>
<td>961</td>
<td>1036</td>
</tr>
</tbody>
</table>

A technique is a simple and orthogonal leverage to effectively shift the analysis cost/precision balance for the better. The technique’s correctness is obvious enough to avoid the burden of a safety proof that would be needed if we newly designed the abstract semantics.

References


